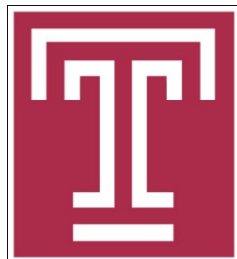




# Network Function Deployment with Balanced Server and Link Resources in Tree Topologies

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# 1. Introduction

- Network Function Virtualization (NFV)
  - Virtualizing network functions into software modules
- Virtualized Network Function (VNF)  
software implementation of network services
  - Improve performance:
    - Web proxy, load balancer
  - Enhance security:
    - Firewall, IDS/IPS
  - Examples:



Web Proxy



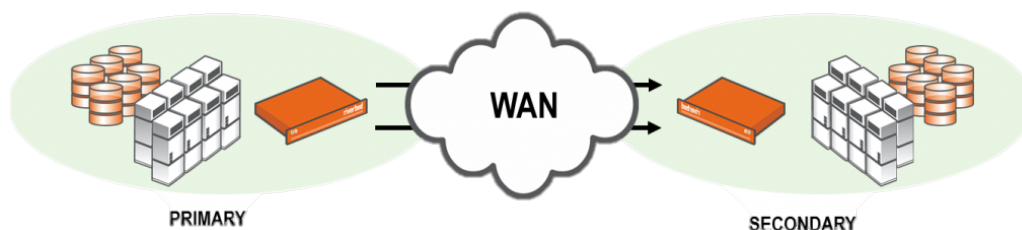
Firewall



NAT

# VNF Traffic Changing Effects [1]

- VNFs may change **flow rates** in different ways
  - Citrix CloudBridge WAN accelerator: 20% (diminishing)



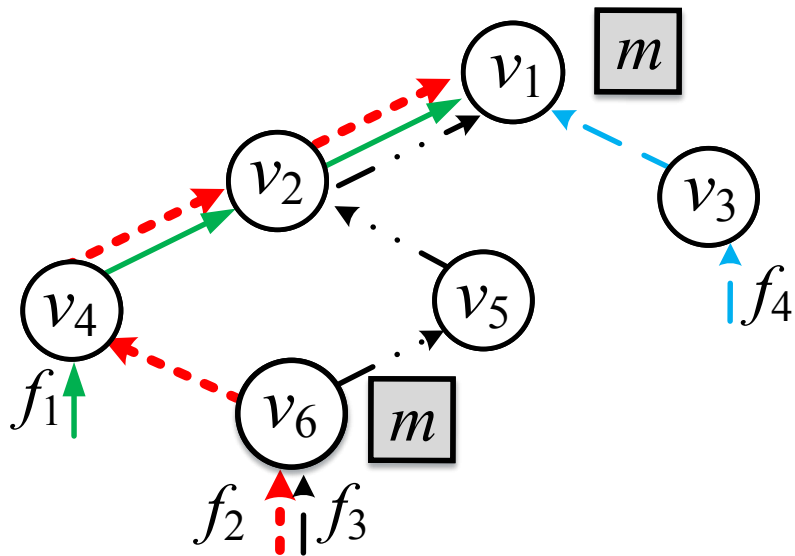
- BCH(63,48) encoder: 130% (expanding)



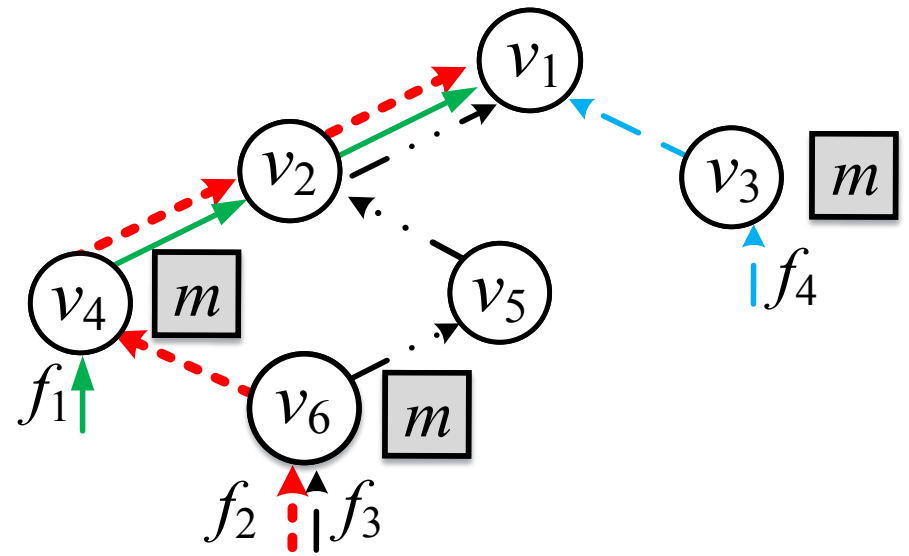
# A motivating example

Traffic-diminishing ratio  
of VNF  $m$ : 0.5

Initial flow rate:  
 $f_1$  (2),  $f_2$  (4),  $f_3$  (2),  $f_4$  (2)



(a) Two VNFs allowed.



(b) Three VNFs allowed.

## 2. Our model



- Problem

- Deploy a single type of VNFs with traffic-diminishing effect into the network

- Objective

- Minimize total bandwidth consumption of all flows on all links along their paths

- Constraint

- Each flow to be processed
- Deploy a limited number of a single type of VNFs

# 3. Problem Formulation

A mathematical optimization problem on minimizing total flow bandwidth consumption

$$\min \quad b(\mathcal{P}) = \sum_{f \in F} b(f) = \sum_{f \in F} \sum_{e \in p_f} b_e(f) \quad (1)$$

$$\text{s.t.} \quad |\mathcal{P}| = \sum_{v \in V} m_v \leq k \quad \forall m \in M \quad (2)$$

$$\sum_{v \in p_f} f_v = 1 \quad \forall f \in F \quad (3)$$

$$f_v \leq m_v \quad \forall v \in V \quad (4)$$

$$m_v = \{0, 1\}, f_v = \{0, 1\} \quad \forall v \in V \quad (5)$$

# 4. Solution for trees

- **Lowest Common Ancestor (LCA)**

- LCA of two vertices  $v$  and  $w$  in an acyclic graph  $G$  is the lowest vertex that has both  $v$  and  $w$  as descendants

- **Solution**

- Greedy Solution for Trees (GST)

- **Steps**

- Deploy one VNF on each leaf
- Merge two VNFs with the minimum difference of the total bandwidth value when we delete two VNFs on  $v$  and  $w$  and place one on  $LCA(v,w)$
- Until total number of deployed VNFs no more than  $k$

## 4. Solution for trees (cont'd)

- Optimality
  - Proof: Induction
- Maintenance of all difference values
  - Min-heap
  - Improve time efficiency
- Time complexity
  - $O(|V|^2 \log |V|)$
  - $|V|$ : #vertices



# 5. Solution for DAGs



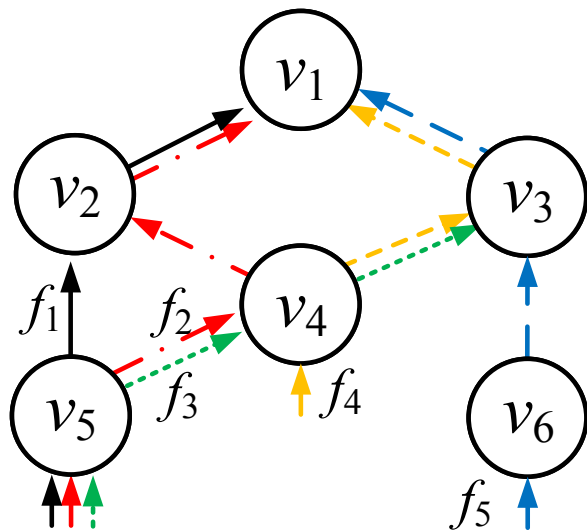
- **Directed Acyclic Graph (DAG)**
  - A finite directed graph with no directed cycles
  - A tree is a special case of a DAG
- **Solution**
  - Directed Acyclic Graph Technique (DAGT)
- **Steps**
  - Deploy one VNF on each all sources of flows
  - Sort all vertices in topological order level by level corresponding to all flows' paths
  - Apply Alg. GST for vertices with the same order

# 5. Solution for DAGs (cont'd)

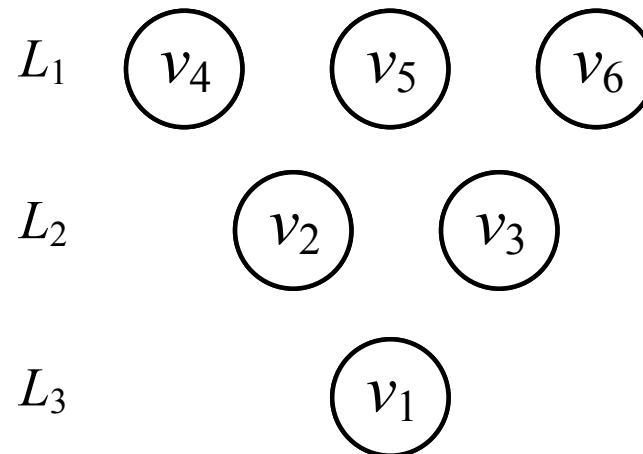
- Time complexity
  - $O(|V|^3 \log |V|)$
  - $|V|$ : #vertices

Traffic-diminishing ratio  
of VNF  $m$ : 0.5

Initial flow rate:  
All are 1



(a) A DAG topology.



(b) Topological order.

# 4. Solution for general topologies

- Decrement function
  - Decrement of the total bandwidth consumption by a deployment plan
- Marginal decrement
  - Additional bandwidth decrement of processing flows by deploying VNFs on a new subset of vertices beyond current deployment
- Decrement function is submodular
  - Proof insight
    - More VNFs are placed, the less bandwidth consumption is, since each flow can be processed no later than the previous placement

# 4. Solution for general topologies (cont'd)

- Solution
  - General Topology Placement (GTP)
- Steps
  - Iteratively select  $v \in V$  with the maximum marginal decrement until all flows are fully served
- Approximation ratio  $\frac{1}{1-\frac{1}{e}}$
- Time complexity
  - $O(k|V| \log |V|)$
  - $|V|$ : #vertices
  - $k$ : limited #VNFs

# 7. Simulation

- Comparison algorithms
  - Random
    - randomly deploy VNFs until it places  $k$  VNFs
  - Best-effort
    - place one VNF on the vertex, which can reduce the total bandwidth of flows mostly, until it places  $k$  VNFs
- Our proposed algorithms
  - Tree: Alg. GST
  - DAG: Alg. DAGT
  - General topo: Alg. GTP

# Settings



- Variables

- VNF number constraint  $k$

- Default value:  $k = 8$  for tree,  $k = 11$  for DAG,  $k = 17$  for the general topo

- Traffic-changing ratio

- Default value: 0.5

- Flow density

- Default value: 0.5

- Topology size

- Default value: 22 for tree, 30 for DAG, 36 for a general topo

- Topology kind

- Metric

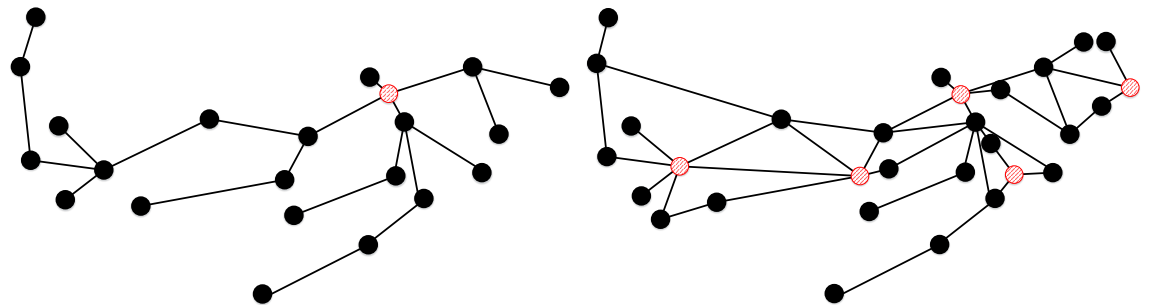
- Total bandwidth consumption of all flows

# Settings

- Topology



(a) The Archipelago (Ark) Infrastructure.



(b) Tree topology (subgraph of (a)). (c) DAG topology (subgraph of (a)).

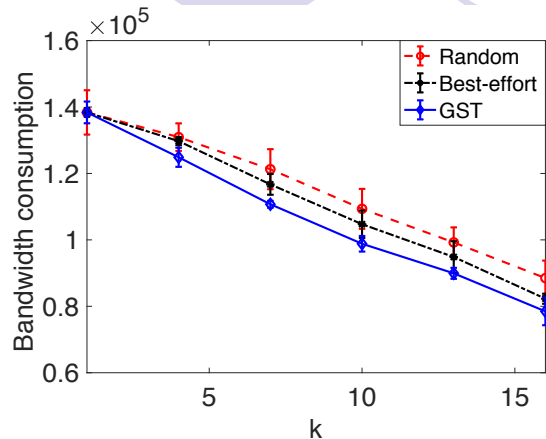
- Middlebox traffic-diminishing ratio

- From 0 (e.g., spam filters) to 0.9 (e.g., traffic optimizer) with a stride of 0.1
- Additional simulation on spam filter

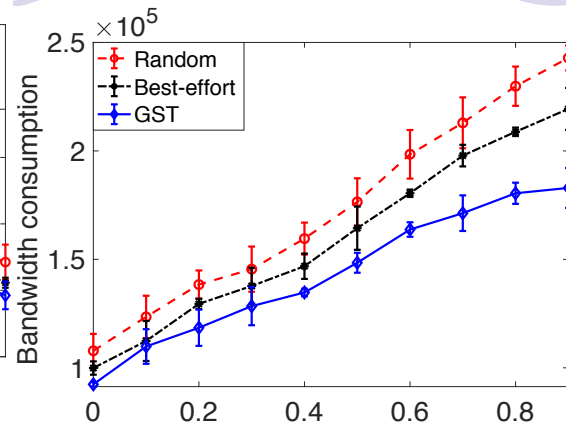
- Flow rate distribution

- CAIDA data center 1-hour packet trace

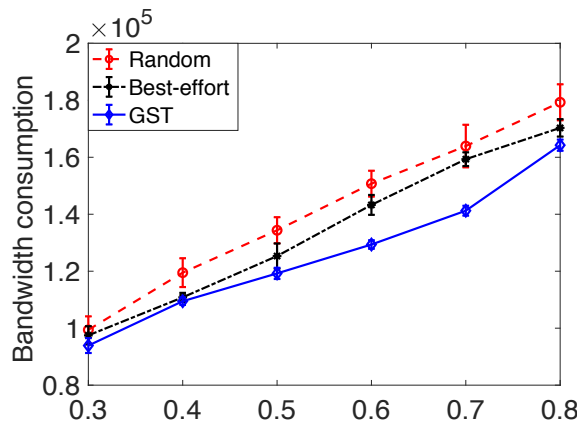
# Simulation results of tree



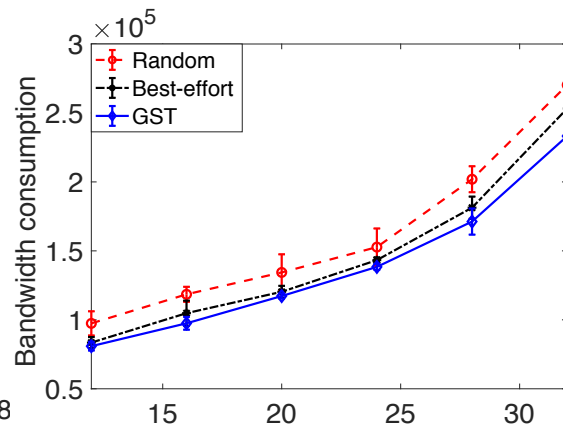
(a) VNF number constraint  $k$ .



(b) Traffic-changing ratio.



(c) Flow density.



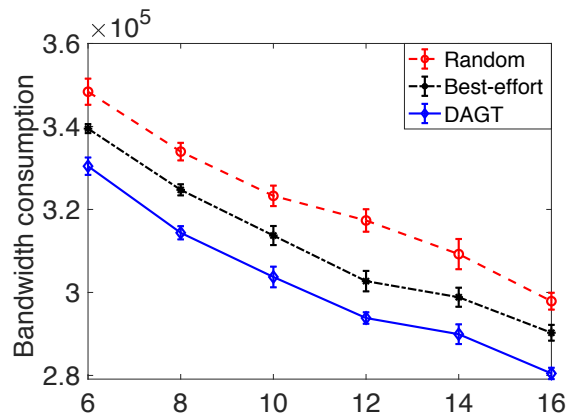
(d) Topology size.

Tree Topology

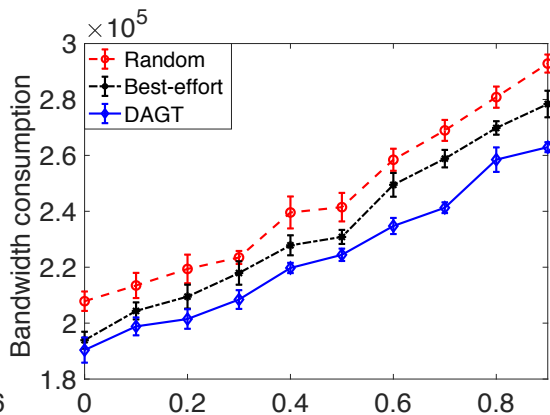
- Alg. GST performs best for all four variables
- $k = 1$ , only one feasible placement plan for all methods
- Traffic-changing ratio has the largest impact on the bandwidth consumption
- Random has the biggest fluctuation



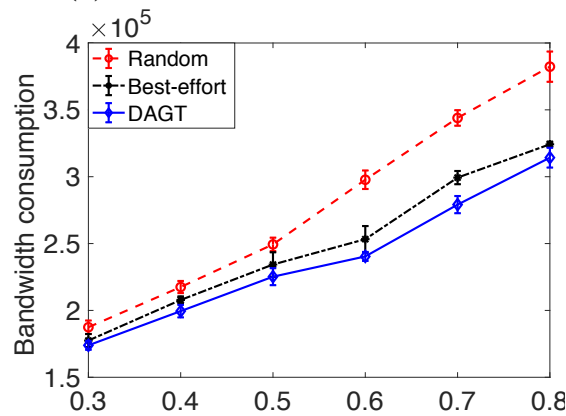
# Simulation results of DAG(cont'd)



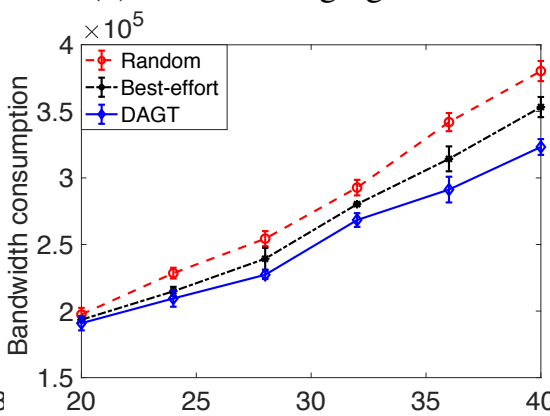
(a) VNF number constraint  $k$ .



(b) Traffic-changing ratio.



(c) Flow density.

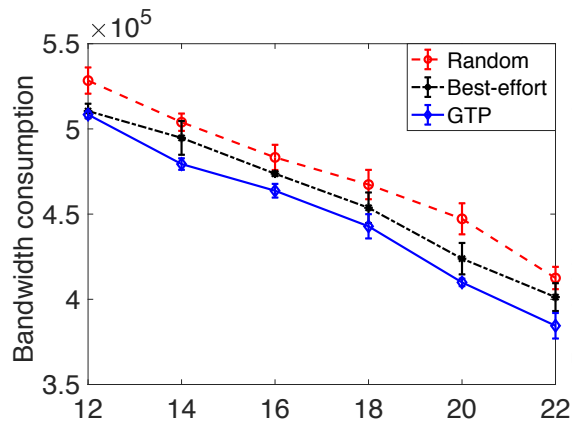


(d) Topology size.

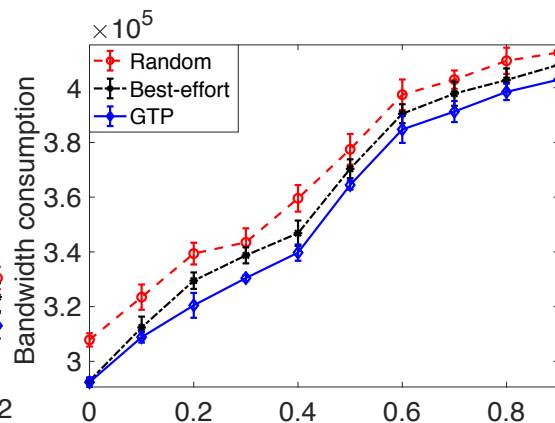
DAG Topology

- Bandwidth consumption is almost three times of tree.
- In Fig. b, bandwidth of DAGT is 85.1% of Random and 92.0% of Best-effort.
- Deviation of DAGT in fig. c is smaller than in last slide
- When the topology size is larger than 35, DAGT performs even better.

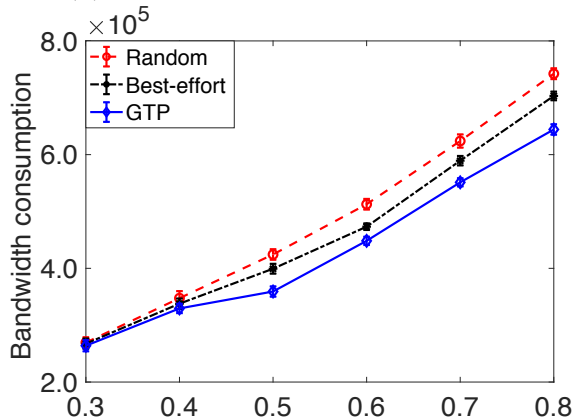
# Simulation results of general topo (cont'd)



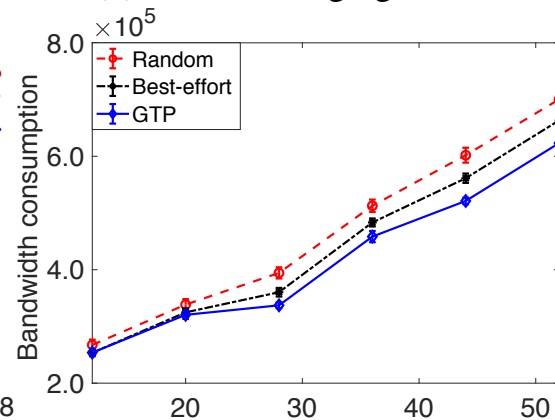
(a) VNF number constraint  $k$ .



(b) Traffic-changing ratio.



(c) Flow density.

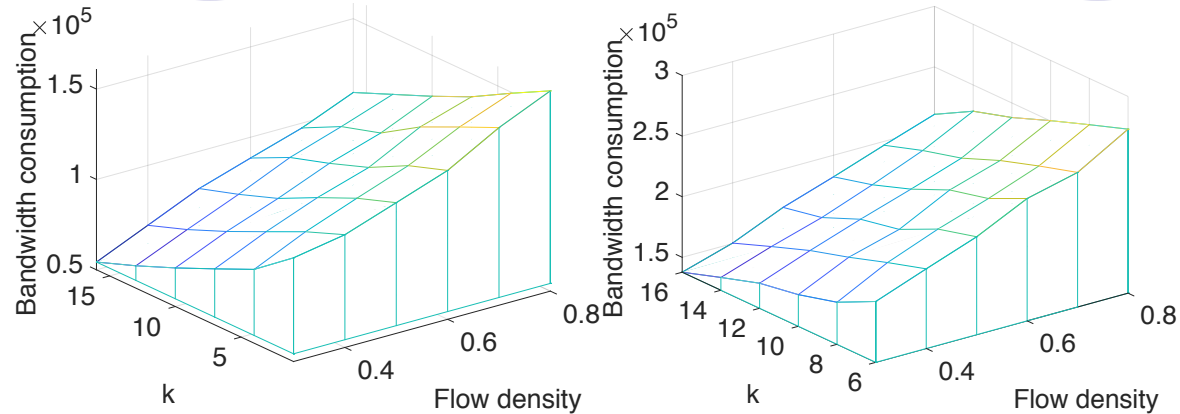


(d) Topology size.

General Topology

- Error bars become shorter than last two slides
- Bandwidth consumption increases faster in fig. b when ratio ranges from 0.4 to 0.6
- When flow density is lower than 0.4 in fig. c, little difference among three algorithms
- Alg. GTP becomes larger when the topology size increases

# Simulation results (cont'd)



(a) Tree.

(b) DAG.

Spam Filter

(Traffic diminishing ratio: 0)

- Flow density plays a more important role in affecting the total bandwidth consumption
- When flow density doubles from 0.3 to 0.6, bandwidth consumption in tree increases 30.2%, while increment is only 25.6% in DAG



# Conclusion and Future Work

- Problem
  - Using limited number of traffic-diminishing VNFs process all flows
- Objective
  - Minimize total bandwidth consumption
- Solutions
  - Tree: optimal
  - Directed Acyclic Graph: efficient heuristic
  - General graph: performance-guaranteed
- Future Work
  - Traffic-expanding VNFs
  - Service chain: an ordered set of multiple VNFs



Questions contact:  
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